

**On completion of this unit successful students will be able**

- state the definition of a Riemannian manifold  $M$  and calculate the length of a curve, and area of a domain in  $M$
- calculate the Riemannian metric on surfaces embedded in  $\mathbf{E}^3$
- define a connection on a manifold, state the Levi-Civita theorem, and calculate the connection for surfaces of cylinder, sphere and cone in  $\mathbf{E}^3$ , and for Lobachevsky (hyperbolic) plane
- state the properties of geodesics on a Riemannian manifold, and calculate the parallel transport of vectors along a geodesics for the sphere and cylinder in  $\mathbf{E}^2$  and for Lobachevsky plane
- state the definition of the Riemann curvature tensor, and calculate the Riemann curvature tensor for some 2-dimensional Riemannian manifolds.